

# Story\_Assignment\_6

2024-11-20

#Noah Krebs

```
library(tidyr)
data <- read.csv("6 ReducingPain.csv")
long_data <- pivot_longer(data,
                           cols = everything(), # Select all columns to reshape
                           names_to = "Condition", # Name for the new variable column
                           values_to = "Score") # Name for the value column

write.csv(long_data, "6_ReducingPain_long.csv", row.names = FALSE)

data_1 <- read.csv("6 ReducingPainLong.csv")
print(data_1)
```

```
##      Treatment PainLevel
## 1 Audiobook          5
## 2 Audiobook          6
## 3 Audiobook          7
## 4 Audiobook          2
## 5 Audiobook          6
## 6 Audiobook          3
## 7 Audiobook          4
## 8 Audiobook          8
## 9 Audiobook          5
## 10 Audiobook         4
## 11      Music          5
## 12      Music          4
## 13      Music          4
## 14      Music          7
## 15      Music          6
## 16      Music          4
## 17      Music          6
## 18      Music          4
## 19      Music          3
## 20      Music          5
## 21 Earphones          4
## 22 Earphones          8
## 23 Earphones          7
## 24 Earphones          6
## 25 Earphones         10
## 26 Earphones          6
## 27 Earphones         10
## 28 Earphones          8
## 29 Earphones          5
## 30 Earphones          6
```

```

#Question 1b
overall_mean <- mean(data_1$PainLevel)

group_means <- tapply(data_1$PainLevel, data_1$Treatment, mean)

n <- table(data_1$Treatment)

group_SS <- sum(n * (group_means - overall_mean)^2)

total_SS <- sum((data_1$PainLevel - overall_mean)^2)

error_SS <- total_SS - group_SS

df_total <- length(data_1$PainLevel) - 1
df_groups <- length(group_means) - 1
df_error <- df_total - df_groups

MS_group <- group_SS / df_groups
MS_error <- error_SS / df_error

F_value <- MS_group / MS_error

p_value <- pf(F_value, df_groups, df_error, lower.tail = FALSE)

print(F_value)

## [1] 5.020101
print(p_value)

## [1] 0.01400622

```

```

#Question 1 c-d
anova <- aov(data_1$PainLevel ~ data_1$Treatment, data = data)
summary(anova)

##              Df Sum Sq Mean Sq F value Pr(>F)
## data_1$Treatment  2   29.6   14.800    5.02  0.014 *
## Residuals       27   79.6    2.948
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

*# Conclusion: Since the p\_value is less than .05, we can conclude that at least one of the three treatments is different from the others.*

```

#Question 1 e-g
group_means <- tapply(data_1$PainLevel, data_1$Treatment, mean)
group_means <- sort(group_means) # Order means from smallest to largest

print(group_means)

```

```
##      Music Audiobook Earphones
##      4.8      5.0      7.0

# Calculate pairwise differences
pairwise_differences <- combn(names(group_means), 2, function(x) {
  diff <- abs(group_means[x[1]] - group_means[x[2]])
  data.frame(pair = paste(x[1], "-", x[2]), difference = diff)
}, simplify = FALSE)
pairwise_differences <- do.call(rbind, pairwise_differences) # Combine into a data frame
print(pairwise_differences)

##                pair difference
## Music      Music - Audiobook    0.2
## Music1     Music - Earphones    2.2
## Audiobook  Audiobook - Earphones  2.0

# Calculate group means for individual observations
group_means_map <- with(data, ave(data_1$PainLevel, data_1$Treatment, FUN = mean))

# Calculate Error SS
error_SS <- sum((data$PainLevel - group_means_map)^2)

# Calculate Error DF
df_error <- nrow(data) - length(group_means)

# Calculate Error MS
MS_error <- error_SS / df_error

cat("Error Mean Square (MS_error):", MS_error, "\n")

## Error Mean Square (MS_error): 0

# Calculate Standard Error (SE) for a specific pair (Audiobook vs Music)
n <- table(data$Treatment)
SE <- sqrt(MS_error * (1 / n["Audiobook"] + 1 / n["Music"]))

cat("Standard Error (SE):", SE, "\n")

## Standard Error (SE): NA

pairwise_differences$q_stat <- pairwise_differences$difference / SE

print(pairwise_differences)

##                pair difference q_stat
## Music      Music - Audiobook    0.2    NA
## Music1     Music - Earphones    2.2    NA
## Audiobook  Audiobook - Earphones  2.0    NA

k <- length(group_means)
critical_q <- qtkey(0.95, k, df_error)
pairwise_differences$p_value <- ptukey(pairwise_differences$q_stat, k, df_error, lower.tail = FALSE)
print(pairwise_differences)

##                pair difference q_stat p_value
## Music      Music - Audiobook    0.2    NA    NA
## Music1     Music - Earphones    2.2    NA    NA
## Audiobook  Audiobook - Earphones  2.0    NA    NA
```

```
anova_result <- aov(data_1$PainLevel ~ data_1$Treatment, data = data)
tukey_result <- TukeyHSD(anova_result)
```

*#After looking at the results I observed a significant difference in the music and earphones comparison.*

*#Question 1*

*#Tukey short*

```
data <- data.frame(
  Treatment = c(rep("Audiobook", 10), rep("Music", 10), rep("Earphones", 10)),
  PainLevel = c(5, 6, 7, 2, 6, 3, 4, 8, 5, 4, 5, 4, 4, 7, 6, 4, 6, 4, 3, 5, 4, 8, 7, 6, 10, 6, 10, 8, 5,
)
aov_res <- aov(formula = PainLevel ~ Treatment, data = data)
summary(aov_res)
```

```
##           Df Sum Sq Mean Sq F value Pr(>F)
## Treatment    2   29.6   14.800    5.02  0.014 *
## Residuals   27   79.6    2.948
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
tukey_res <- TukeyHSD(x = aov_res, ordered = TRUE, conf.level = 0.95)
print(tukey_res)
```

```
##      Tukey multiple comparisons of means
##      95% family-wise confidence level
##      factor levels have been ordered
##
## Fit: aov(formula = PainLevel ~ Treatment, data = data)
##
## $Treatment
##              diff          lwr          upr          p adj
## Audiobook-Music    0.2 -1.70387901 2.103879 0.9633444
## Earphones-Music    2.2  0.29612099 4.103879 0.0210755
## Earphones-Audiobook 2.0  0.09612099 3.903879 0.0380535
```

*#Question 2*

*#Part A*

```
effect_difference <- 0.5 # Smallest difference to detect
error_ms <- 6.5         # Error Mean Square
alpha <- 0.05           # Significance level
power <- 0.9            # Desired power
num_groups <- 4         # Number of streams
```

```
f <- effect_difference / sqrt(error_ms)
```

```
group_means <- c(0, 0.5, 1.0, 1.5)
overall_mean <- mean(group_means)
```

```
n <- 2
achieved_power <- 0
```

```
while (achieved_power < power) {
  total_sample_size <- n * num_groups
  df1 <- num_groups - 1
```

```

df2 <- total_sample_size - num_groups

ncp <- n * sum((group_means - overall_mean)^2) / error_ms

f_crit <- qf(p=alpha, df1=df1, df2=df2, lower.tail=FALSE)

achieved_power <- pf(q=f_crit, df1=df1, df2=df2, ncp=ncp, lower.tail=FALSE)

if (achieved_power < power) {
  n <- n + 1
}
}
print(n)

```

```
## [1] 75
```

*#Question 2*

*# Part B*

*#To reach a power of at least .9, one has to take 4 groups of 75 samples.*

*#300 total*

*#Each sample of tag cost \$25*

*#300x25 = \$7500 which is less than 100,000. You will be able to complete the experiment with the desire*